



## Barnfields Primary School

### Calculation Progression Policy

#### Rationale

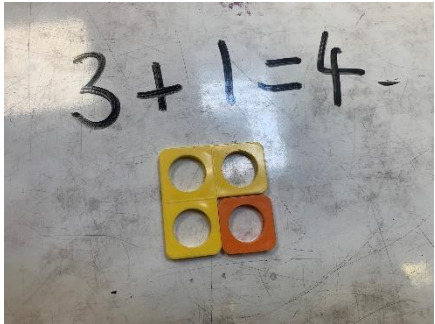

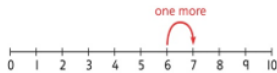
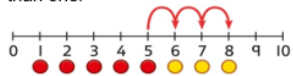
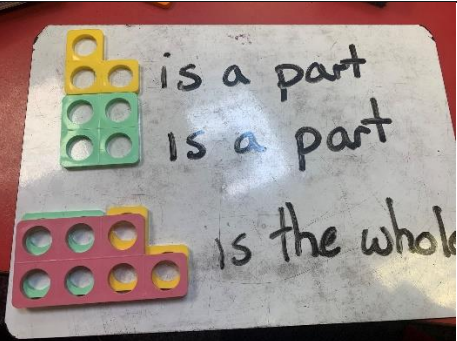

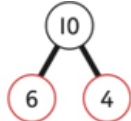
At Barnfields Primary School, we believe in equipping all of our children to become fluent and proficient Mathematicians. The aim of this Calculation Progression Policy is to ensure all of our children are able to use a range of mental calculation strategies effectively, efficiently and flexibly. In partnership with this, it is imperative that children can also use a range of written methods accurately and appropriately. When children are able to employ both of these strategies effectively, they can then solve problems and reason mathematically efficiently. Underpinning all this, is the belief that all children can acquire a competent and confident understanding of numbers and the number system combined with an instant recall of a set of age-appropriate number facts. This knowledge and skillset combined with the automaticity of known facts will ensure our children are able to explore Maths in depth and with success using appropriate vocabulary and skills in order to do so effectively.

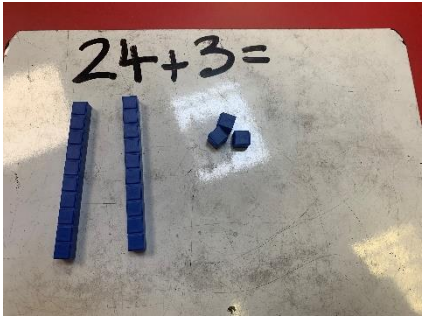
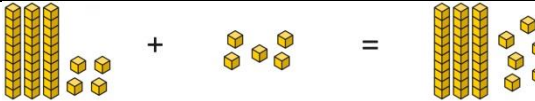
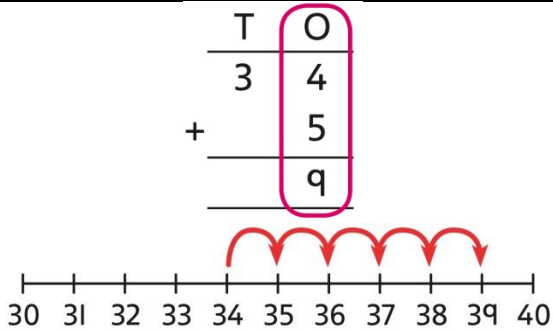
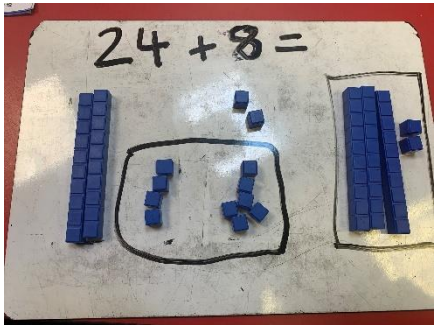
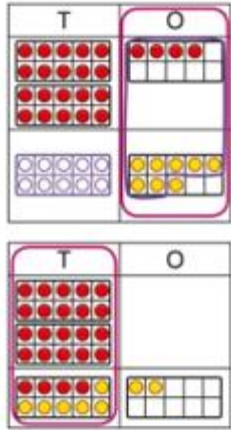


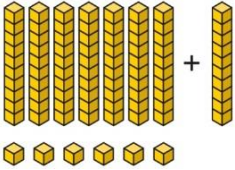
#### Concrete, Pictorial, Abstract approach

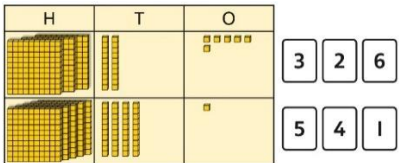
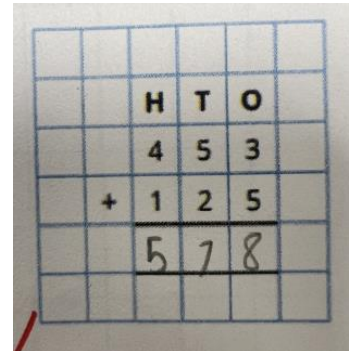
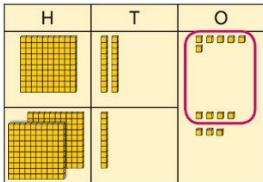
The Concrete, Pictorial, Abstract approach (CPA) is a highly effective approach to teaching that develops a deep and sustainable understanding of maths in pupils. It is an essential technique within the Singapore method of teaching maths for mastery which is now used to teach Maths in the majority of schools across the UK and employed at Barnfields Primary School. Children can find Maths difficult because it is abstract. The CPA approach builds on children's existing knowledge by introducing abstract concepts in a concrete and tangible way. It involves moving from concrete materials, to pictorial representations, to abstract symbols and problems. Concrete is the "doing" stage. During this stage, students use concrete objects to model problems. Unlike traditional maths teaching methods where teachers demonstrate how to solve a problem, the CPA approach brings concepts to life by allowing children to experience and handle physical (concrete) objects. With the CPA framework, every abstract concept is first introduced using physical, interactive concrete materials.

- Concrete is the "doing" stage. During this stage, children use concrete objects to model problems. Unlike traditional maths teaching methods where teachers demonstrate how to solve a problem, the CPA approach brings concepts to life by allowing children to experience and handle physical (concrete) objects.
- Pictorial is the "seeing" stage. Here, visual representations of concrete objects are used to model problems. This stage encourages children to make a mental connection between the physical object they just handled and the abstract pictures, diagrams or models that represent the objects from the problem. Building or drawing a model makes it easier for children to grasp difficult abstract concepts (for example, fractions). Simply put, it helps students visualise abstract problems and make them more accessible.
- Abstract is the "symbolic" stage, where children use abstract symbols to model problems. Students will not progress to this stage until they have demonstrated that they have a solid understanding of the concrete and pictorial stages of the problem. The abstract stage involves the teacher introducing abstract concepts (for example, mathematical symbols). Children are introduced to the concept at a symbolic level, using only numbers, notation, and mathematical symbols (for example,  $+$ ,  $-$ ,  $\times$ ,  $\div$ ) to indicate addition, multiplication or division.

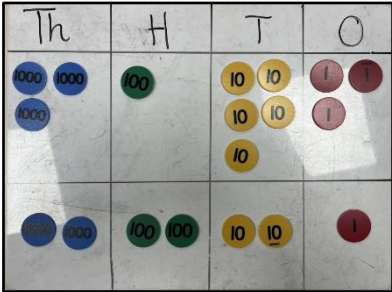
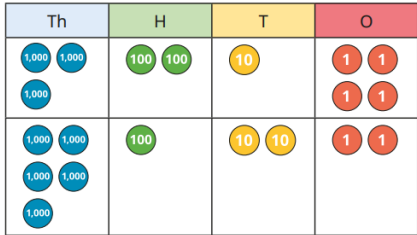
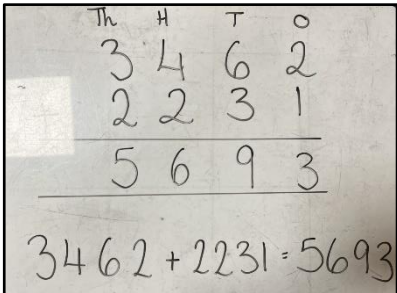
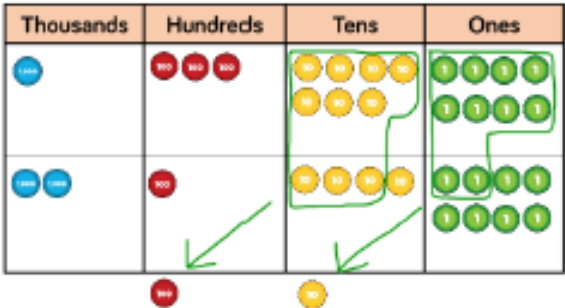
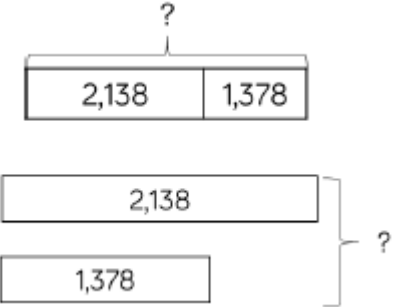
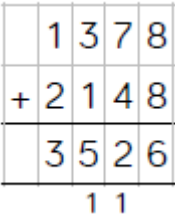
It is important to note this is not a linear approach and teachers will move back and forth between the CPA stages as required.

Year 1 addition			
Concept	Concrete	Pictorial	Abstract
Counting and adding more		<p>Children add one more cube or counter to a group to represent one more</p>  <p><i>One more than 4 is 5.</i></p>	<p>Use a number line to understand how to link counting on with finding one more.</p>  <p><i>One more than 6 is 7. 7 is one more than 6.</i></p> <p>Learn to link counting on with adding more than one.</p>  <p><math>5 + 3 = 8</math></p>
Understanding part-part-whole relationship		<p>Here are some frogs.</p> <ul style="list-style-type: none"> <li>▶ Can you see two groups of frogs?</li> <li>▶ How many frogs are in each group?</li> <li>▶ Complete the sentences.</li> </ul> <p>_____ is a part. _____ is a part. The whole is _____</p> 	 <p><math>6 + 4 = 10</math></p>

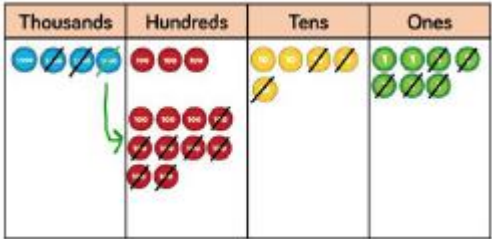
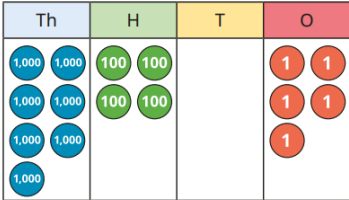

Year 2			
Addition			
Concept	Concrete	Pictorial	Abstract
Adding a 1-digit number to a 2-digit number not bridging a 10		 <p>34 is 3 tens and 4 ones. 4 ones and 5 ones are 9 ones. The total is 3 tens and 9 ones.</p>	
Adding a 1-digit number to a 2-digit number with an exchange		<p>Exchange 10 ones for 1 ten.</p> 	<p>Exchange 10 ones for 1 ten.</p> 
Adding a multiple of 10 to a 2 digit number	<p>Add the 10s and then recombine.</p>  <p>27 is 2 tens and 7 ones. 50 is 5 tens.</p>	<p>Add the 10s and then recombine.</p> 	<p>Add the 10s and then recombine.</p> <p><math>37 + 20 =</math></p> <p><math>30 + 20 = 50</math></p>

Y3 Addition			
Concept	Concrete	Pictorial	Abstract
Add numbers with up to three digits using the formal written method of column addition- no regrouping	<p>Use place value equipment to make a representation of a calculation. This may or may not be structured in a place value grid.</p> <p><i>326 + 541 is represented as:</i></p> 	<p>Represent the place value grid with equipment to model the stages of column addition.</p>	<p>Use a column method to solve efficiently, using known bonds. Children must understand how this relates to place value at every stage of the calculation.</p> 
Add numbers with up to three digits using the formal written method of column addition- with regrouping	<p>Use place value equipment to enact the exchange required.</p>  <p><i>There are 13 ones. I will exchange 10 ones for 1 ten.</i></p>	<p>Model the stages of column addition using place value equipment on a place value grid.</p>	<p>Use column addition, ensuring understanding of place value at every stage of the calculation.</p>

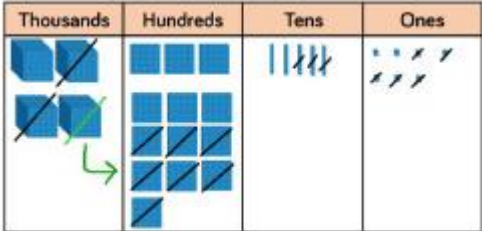
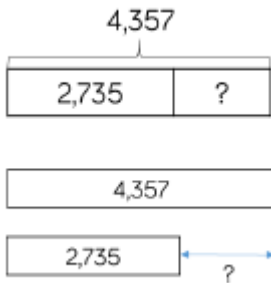
## Year 4 Addition

Concept	Concrete	Pictorial	Abstract
Add up to two 4 digit numbers with no exchange.		<p>Calculate <math>3,214 + 5,122</math></p> <p>Use the place value chart to help you.</p> 	
Add two 4 digit numbers with exchanges.			

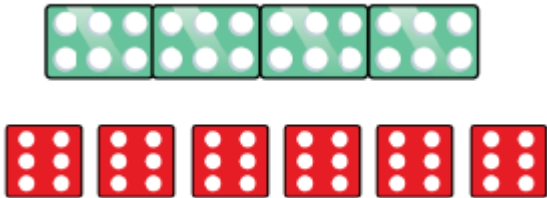
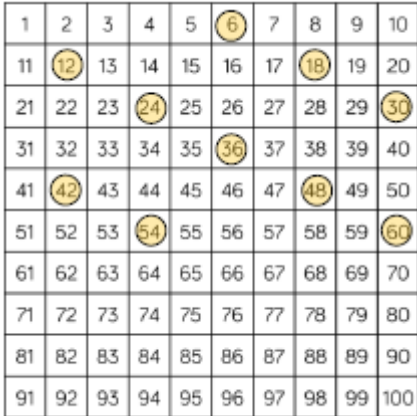
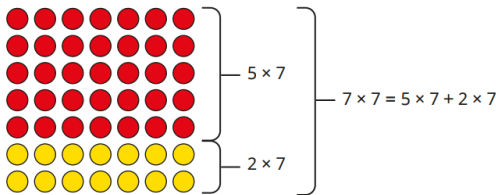

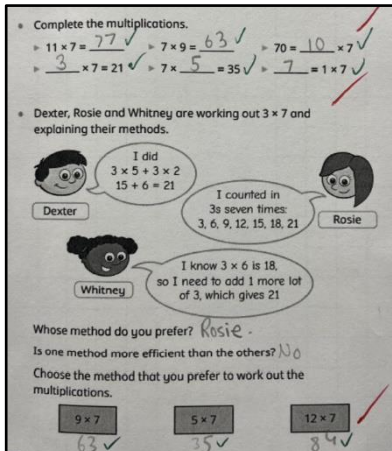
## Year 4 Subtraction

Concept	Concrete	Pictorial	Abstract
Subtract two 4 digit numbers- no exchange		<p>c) <math>7,405 - 404</math></p> 	

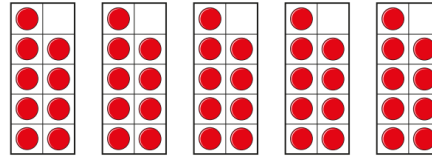
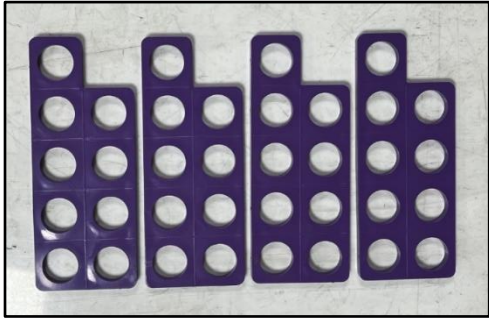


Subtract two 4 digit numbers- with exchanges			$\begin{array}{r} 4357 \\ - 2735 \\ \hline 1622 \end{array}$
--	---	---	--

### Year 4 Multiplication

Concept	Concrete	Pictorial	Abstract
Recall and apply multiplication and division facts for 6 times tables			$3 \times 6 = 18$ $6 \times 3 = 18$ $18 \text{ divided by } 3 = 6$ $18 \text{ divided by } 6 = 3$
Recall and apply multiplication and division facts for 7 times tables			

Recall and apply multiplication and division facts for 9 times tables



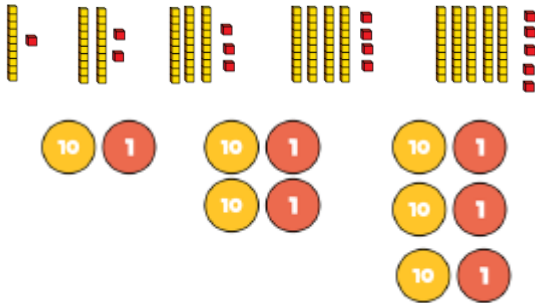
$$7 \times 9 = 63$$

$$3 \times 9 = 27$$

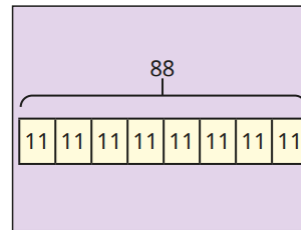
$$9 \times 9 = 81$$

$$12 \times 9 = 108$$

Recall and apply multiplication and division facts for 11 times tables



1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

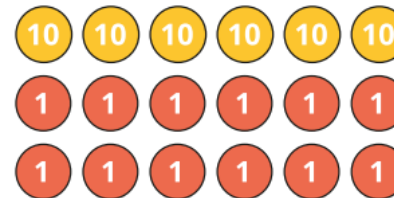


$$99 \div 11$$

$$55 \div 11$$

$$22 \div 11$$

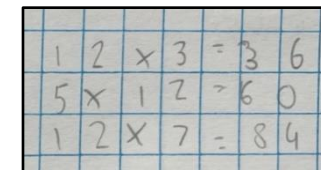
Recall and apply multiplication and division facts for 12 times tables



$$36 \div 12$$

$$60 \div 12$$

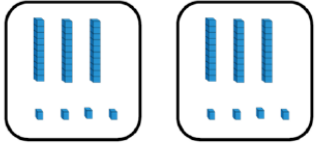
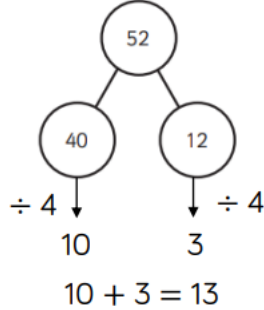
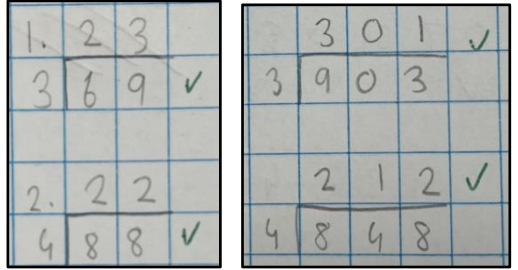
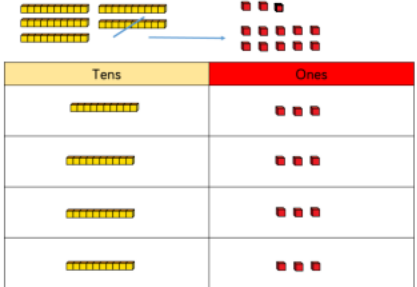
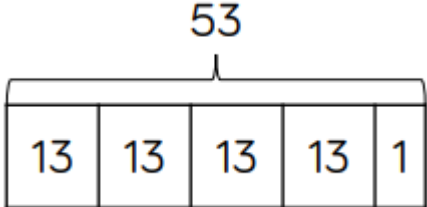
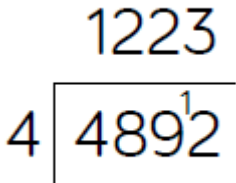
$$84 \div 12$$



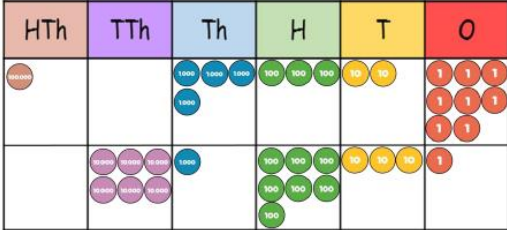
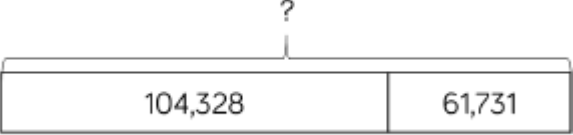
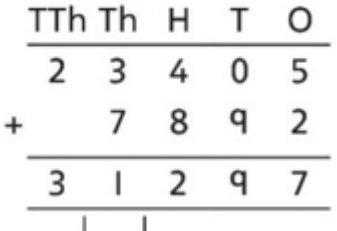
Use informal written methods for multiplication	<div><div><div>Tens</div><div>Ones</div></div><div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div><div></div></div></div></div><div><div><div><div>24 × 3 = 12 + 60 = 72</div></div></div></div></div>	<div><div>34 × 6 = 204</div><div><div>10 × 6 = 60</div><div>10 × 6 = 60</div><div>10 × 6 = 60</div><div>4 × 6 = 24</div></div><div><div>0</div><div>60</div><div>120</div><div>180</div><div>204</div></div></div>	<div><div>24 × 8 = 192</div><div><div>24</div><div><div>20</div><div>4</div></div><div><div>× 8</div><div>× 8</div></div><div><div>160</div><div>32</div></div><div><div>160 + 32 = 192</div></div></div></div>
Multiply up to 3 digit number by a 1 digit number- no exchange	<div><div>Use place value equipment to make multiplications.</div><div><div>Make 4 × 136 using equipment.</div><div><div><div>100</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div><div><div>100</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div><div><div>100</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div><div><div>100</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div></div></div></div>	<div><div><div><div>100</div><div>100</div><div>100</div><div>10</div><div>1</div><div>1</div></div><div><div>100</div><div>100</div><div>100</div><div>10</div><div>1</div><div>1</div></div><div><div>100</div><div>100</div><div>100</div><div>10</div><div>1</div><div>1</div></div></div></div>	<div><div><div>312</div><div>×</div><div>3</div><div>936</div></div></div>
Multiply a 3 digit number by a 1 digit number with exchanges	<div><div><div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div><div><div><div></div><div></div><div></div><div></div></div><div><div></div><div></div><div></div><div></div></div></div></div><div><div>245 × 4 =</div></div></div>	<div><div><div><div>Hundreds</div><div>Tens</div><div>Ones</div></div><div><div><div>100</div><div>100</div><div>100</div><div>100</div></div><div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div><div>10</div></div><div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div><div>1</div></div></div><div><div>100</div><div>10</div><div>10</div></div></div></div>	<div><div><div><div>H</div><div>T</div><div>O</div></div><div><div>2</div><div>4</div><div>5</div></div><div><div>×</div><div></div><div></div><div>4</div></div><div><div>9</div><div>8</div><div>0</div></div><div><div>1</div><div>2</div></div></div></div>

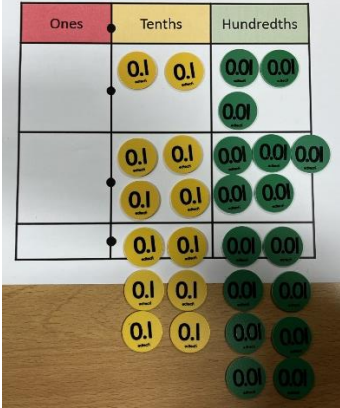
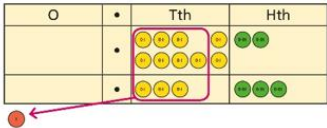


# Year 4 Division

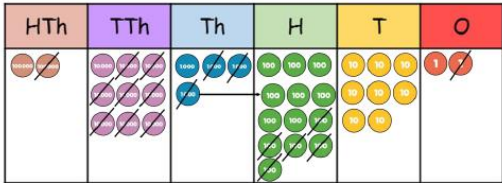
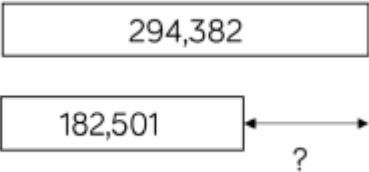
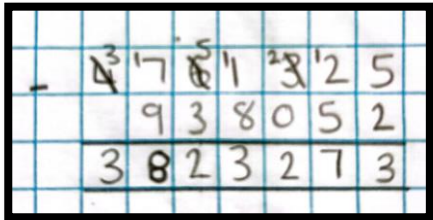
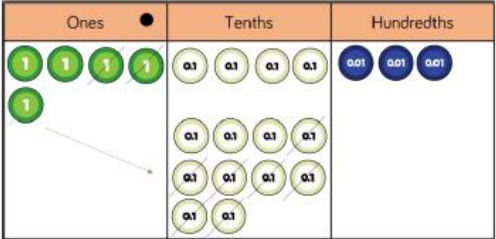
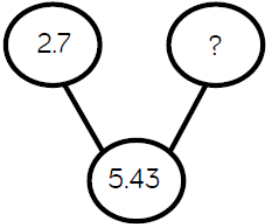
Concept	Concrete	Pictorial	Abstract
Divide 2 and 3 digit numbers using formal written method of short division	 $68 \div 2 = 34$		
Divide 2 and 3 digit numbers using formal written method of short division- with remainders			

# UKS2 Addition

Concept	Concrete	Pictorial	Abstract
Add whole numbers with more than 4 digits using formal written methods			

<p>Add numbers with up to 3 decimal places using formal written methods</p>		 $\begin{array}{r} \text{O} \cdot \text{Tth} \text{Hth} \\ 0 \cdot 9 \quad 2 \\ + 0 \cdot 3 \quad 3 \\ \hline 1 \cdot 2 \quad 5 \\ \hline \end{array}$	$\begin{array}{r} \text{O} \cdot \text{Tth} \text{Hth} \\ 0 \cdot 9 \quad 2 \\ + 0 \cdot 3 \quad 3 \\ \hline 1 \cdot 2 \quad 5 \\ \hline \end{array}$
---	---	---	---

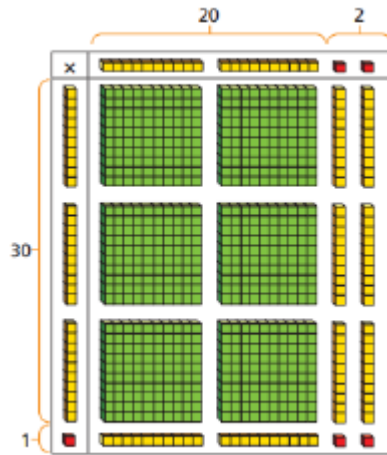
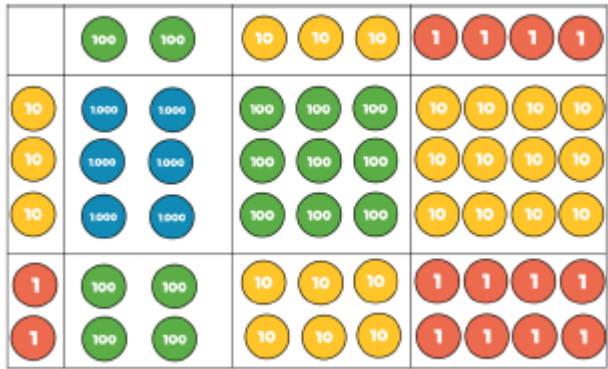
### UKS2 Subtraction

Concept	Concrete	Pictorial	Abstract
<p>Subtract whole numbers with more than 4 digits using formal written methods</p>			
<p>Subtract numbers with up to 3 decimal places</p>			$\begin{array}{r} 5.43 \\ - 2.7 \\ \hline 2.73 \end{array}$

### UKS2 Multiplication

Concept	Concrete	Pictorial	Abstract
---------	----------	-----------	----------

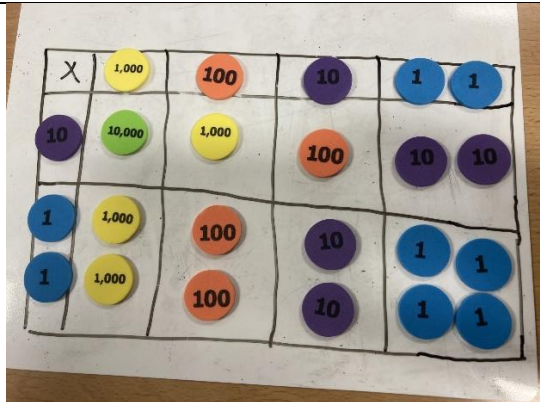
Multiply numbers with up to 4 digits by a 2 digit number using an expanded formal written method (Year 5)



×	200	30	4
30	6,000	900	120
2	400	60	8

	T	H	T	O
1	2	0	0	
2	1	2	0	0
3	1	8	0	
4	1	8	0	
5	1	5	1	8
6	1	5	1	8

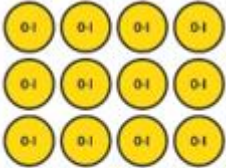


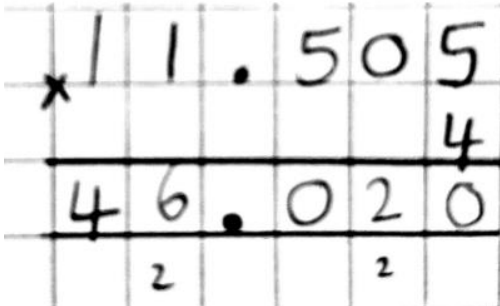

Multiply numbers with up to 4 digits by a 2 digit number using a compact formal written method (Year 5)



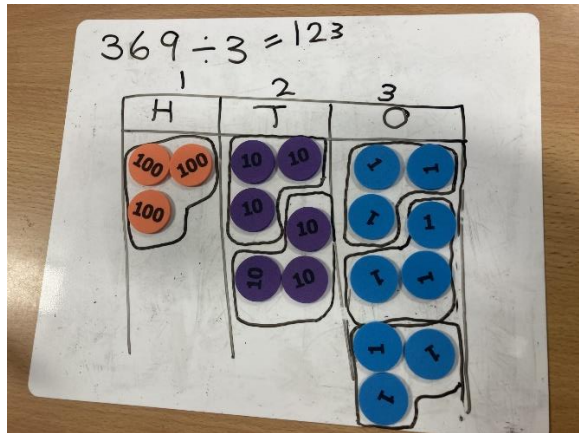
×	1	2	3	5
2	2	4	7	0
2	5	9	3	5

Multiply multi-digit numbers up to 4 digits by a 2 digit whole number using the formal written method of long

TTh	Th	H	T	O
	2	7	3	9
×			2	8
2	1	9	1	2
2	5	3	7	
5	4	7	8	0
1		1		
7	6	6	9	2

multiplication (Y6)											
Multiplying decimals (Year 6)	 <p>3 groups of 4 tenths is 12 tenths. 4 groups of 3 tenths is 12 tenths.</p>	<p>Represent calculations on a place value grid.</p> <p><math>3 \times 3 = 9</math> <math>3 \times 0.3 = 0.9</math></p> <table border="1" data-bbox="987 389 1370 572"> <tr> <th>T</th><th>O</th><th>•</th><th>Tth</th></tr> <tr> <td></td><td></td><td></td><td>  </td></tr> </table>	T	O	•	Tth					
T	O	•	Tth								
											

UKS2 Division

Concept	Concrete	Pictorial	Abstract																																										
Divide up to 4 digit numbers by a 1 digit number using the formal written method of short division and interpret remainders according to context.		<table border="1" data-bbox="1021 740 1476 1185"><thead><tr><th>Th</th><th>H</th><th>T</th><th>O</th></tr></thead><tbody><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr><tr><td></td><td></td><td></td><td></td></tr></tbody></table>	Th	H	T	O																													<table border="1" data-bbox="1729 748 1989 853"><tbody><tr><td></td><td>4</td><td>2</td><td>6</td><td>6</td></tr><tr><td>2</td><td>8</td><td>5</td><td>13</td><td>12</td></tr></tbody></table>		4	2	6	6	2	8	5	13	12
Th	H	T	O																																										
	4	2	6	6																																									
2	8	5	13	12																																									

Dividing by a 2 digit number using factors (Y6)

Understand that division by factors can be used when dividing by a number that is not prime.

Use factors and repeated division.

$$1,260 \div 14 = ?$$



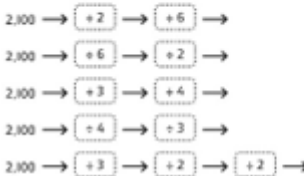
$$1,260 \div 2 = 630$$

$$630 \div 7 = 90$$

$$1,260 \div 14 = 90$$

Use factors and repeated division where appropriate.

$$2,100 \div 12 = ?$$



Dividing by a 2 digit number using long division (Y6)

$$7,335 \div 15 = 489$$

	0	4	8	9	
15	7	3	3	5	
-	6	0	0	0	(x400)
	1	3	3	5	
-	1	2	0	0	(x80)
		1	3	5	
-		1	3	5	(x9)
				0	

- 1 x 15 = 15
- 2 x 15 = 30
- 3 x 15 = 45
- 4 x 15 = 60
- 5 x 15 = 75
- 10 x 15 = 150

Dividing by a 2 digit number using long division with remainders (Y6)

$$372 \div 15 = 24 \text{ r}12$$

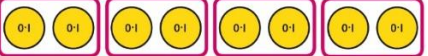
			2	4	r	1	2	
1	5	3	7	2				
-	3	0	0					
		7	2					
-		6	0					
			1	2				

- 1 x 15 = 15
- 2 x 15 = 30
- 3 x 15 = 45
- 4 x 15 = 60
- 5 x 15 = 75
- 10 x 15 = 150

			2	4	$\frac{4}{5}$
1	5	3	7	2	
-	3	0	0		
		7	2		
-		6	0		
			1	2	

$$372 \div 15 = 24 \frac{4}{5}$$

Dividing decimals (Y6)



Use place value equipment to divide decimals into equal groups.  
8 tenths divided into 4 groups. 2 tenths in each group.

0.8			
?	?	?	?

$$4 \times 2 = 8 \quad 8 \div 4 = 2$$

So,  $4 \times 0.2 = 0.8 \quad 0.8 \div 4 = 0.2$

